EVALUATION OF A BUNDLING TECHNIQUE FOR PARALLEL COORDINATES

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Abstract: We present a controlled user study evaluating the effectiveness of bundled curve representations in parallel-coordinates plots. Replacing the traditional $C^0$ polygonal lines by $C^1$ continuous piecewise Bézier curves makes it easier to visually trace data points through each coordinate axis. The resulting Bézier curves can then be bundled to visualize data with given cluster structures. Our results show that: 1) compared to polygonal lines, bundled curves are equally capable of revealing correlations between neighboring data attributes; 2) the geometric cues of bundles can be effective in displaying cluster information.

1 INTRODUCTION

Parallel coordinates are a popular technique for transforming multidimensional data into a 2D image (Inselberg, 1985; Inselberg and Dimsdale, 1990). The $m$-dimensional data items are represented as 2D lines crossing $m$ parallel axes, each axis corresponding to one dimension of the original data. This technique has been incorporated into several data visualization and analysis tools, including XLSTAT\textsuperscript{1} and GGobi (Cook and Swayne, 2003). However, experience has shown several problems with the traditional parallel-coordinates technique. First, the zig-zagging polygonal lines (or polylines, for short) used for data representation are only $C^0$ continuous. They generally lose visual continuation across the parallel-coordinates axes, making it difficult to follow lines that share a common point along an axis—this is known as the cross-over problem. Second, when two or more data points have the same or similar values for a subset of the attributes, the corresponding polylines may overlap and clutter the visualization. This artifact may occur even for medium-sized datasets with a few thousand points. Finally, clusters and related internal structure of the data are not represented in the geometry of the plot, except for implicit visual clustering based on proximity of polylines at the axes.

Several solutions have been proposed for these problems. The cross-over problem has been mitigated by replacing polylines with smooth curves (Theisel, 2000; Graham and Kennedy, 2003; Moustafa and Wegman, 2006; Yuan et al., 2009; Holten and van Wijk, 2010) that interpolate the original values at the axes. Cluster perception in parallel coordinates has been facilitated using edge bundling (Holten, 2006; Zhou et al., 2008; McDonnell and Mueller, 2008; Heinrich et al., 2011b), where curves of the same cluster are grouped geometrically. In contrast to the traditional color-coding of clusters, the resulting curve bundles also reduce visual clutter by freeing up plot space to provide an overview of the data.

While variants of polylines and curves have been evaluated (see Table 1), no prior study evaluated the joint effect of these two features on the perception of clusters and correlations. To fill this gap, we conducted a controlled user study to compare the effectiveness of polylines and curve bundling with respect to cluster perception and correlation judgment.

The study showed that curve bundling maintains the users’ ability to recognize correlation between data attributes, a traditional strength of parallel coordinates. Furthermore, for revealing clusters to the user, curve bundling is at least on par with color coding, the traditional way of representing clusters. Figure 1 compares the polyline version of parallel coordinates with a version using bundled curves.

\footnote{\url{http://www.xlstat.com}}
Figure 1: The cars (Ramos and Donoho, 1983) data displayed as (a) polyline and (b) and bundled plots (Heinrich et al.,
2011b). Data are clustered by number of engine cylinders (4, 6, or 8). In the bundled plot, bundling was \( \beta = 0.95 \) and
cluster centroids were plotted at their projected values on the bundle axis. The adjectives above each value axis indicate the
interpretation of values closer to the axis top.

2 Related Work

In parallel-coordinates visualization, points in \( m \)-dimensional space are represented as lines crossing \( m \)
parallel axes in 2D, so there is no inherent limit on dimensionality. The process of discovering multivariate relations in a
dataset is transformed to a 2D pattern recognition problem. Parallel coordinates were introduced by Inselberg (1985; 1990; 2009), and extended

Traditional parallel coordinates suffer from several problems, especially for large datasets. One issue is the potentially heavy over-plotting of lines, resulting in visual clutter. A proposed remedy is to replace fully opaque, rasterized lines by a density representation of the plotted lines (Miller and Wegman, 1991; Wegman and Luo, 1997). This idea has been adopted for frequency plots (Rodrigues et al., 2003), gray-scale mappings in density plots (Artero et al., 2004), and high-precision textures in combination with transfer functions (Johansson et al., 2005). For continuous data, line density can also be computed analytically using an appropriate reconstruction kernel (Heinrich and Weiskopf, 2009) or by splatting (Heinrich et al., 2011a).

The cross-over problem for polylines arises when two or more lines share common points on an axis. Several authors have solved this by using smooth curves. Theisel (2000) proposes a cubic B-splines model, while Graham and Kennedy (2003) choose a quadratic or cubic curve for a particular section depending on the shape formed by that section and the two adjacent sections. Moustafa and Wegman (2006) build smooth curves by replacing the piecewise linear interpolation of polylines by interpolation via higher-order sinusoidal functions. Others (Holten and van Wijk, 2010; Heinrich et al., 2011b) add a parameter to the spline-based models (Graham and Kennedy, 2003; Yuan et al., 2009) to control the amount of smoothing. All these techniques guarantee curve smoothness, alleviating the cross-over problem by giving different trajectories to points that intersect at an axis. This allows the analyst to reliably connect the curves on either side of the axis.

Visual clutter can also be reduced by preprocessing the data with a clustering algorithm (Jain and Dubes, 1988). The clusters can then be displayed by extensions of parallel coordinates (Fua et al., 1999; Wegman and Luo, 1997; Berthold and Hall, 2003). Whereas early clustering work focused on reducing the amount of displayed data by displaying only markers of entire clusters, recent work has instead focused on displaying all the data and revealing details of the internal structure of clusters. Johansson et al. (2005) combine specific transfer functions for density plots with feature animation, showing both an overview of the data and the inner structure of its clusters. Novotny and Hauser (2006) extend such cluster-based parallel-coordinates visualization to additionally display outliers and trends. Zhou et al. (2009) detect clusters by splatting lines and applying a Gaussian weight to proximate lines.

Other approaches use geometric proximity of lines or curves to represent clusters in parallel coordi-
nates (Zhou et al., 2008; McDonnell and Mueller, 2008; Heinrich et al., 2011b). Zhou et al. (2008) deform traditional polylines by applying attracting and repelling forces. By construction, their method is based on proximity between the initial polylines and, thus, achieves an implicit, yet fixed type of clustering. Their method emphasizes the proximity of the polylines, rather than showing externally provided clusters. Moreover, their visual clustering is based on a piecewise model: the vicinity of polylines between two neighboring data axes (or dimensions) of the parallel-coordinates plot governs the visual clustering between those two data dimensions; other pairs of neighboring data dimensions are clustered independently. Therefore, high-dimensional data is not clustered on a per-data-point level, but based on pairs of data dimensions. The resulting visual clustering is thus sensitive to the order of data dimensions in the parallel-coordinates plot.

Holten introduced edge bundling of tree layouts (Holten, 2006). McDonnell and Mueller (2008) built on this idea, developing a geometric, spline-based approach to computing visual bundling. Their technique targets illustrative parallel-coordinate plots, using visual simplification and non-photorealistic rendering techniques such as silhouette lines, halos, and shadows. Details of the internal structure of data points within clusters as well as correlation are not a focus of their research. Moreover, cluster membership information is based on color coding.

For the user study conducted in this paper, we use a complementary, geometry-based visualization of clusters that we describe in a technical report (Heinrich et al., 2011b). This method improves upon the proximity-based parallel-coordinates techniques of McDonnell and Mueller (2008) and Zhou et al. (2008) in the following ways. First, it makes better use of the available screen space by re-distributing visually clustered curves in a uniform way. Therefore, there is much less overlap in the important parts of the plots—in the regions between two data axes, where users identify correlation of data points. In addition, overdraw and cluttering issues are reduced by this redistribution. Second, $C^1$ continuity of the curved lines across data axes is guaranteed, addressing the crossover problem. For a detailed description of the algorithm and its parameters to control the visualization process, we refer to the paper by Heinrich et al. (2011b).

There have been few previous papers providing user studies on parallel coordinates. Li et al. (2010) compare polyline parallel coordinates and scatterplots. Lanzenberger et al. (2005) investigate the effectiveness of stardinates and parallel-coordinates plots applied to an example data set with psychotherapeutical data. Henley et al. (2007) evaluate scatterplots and parallel coordinates for the task of comparing genomic sequences. A tiled parallel-coordinates technique for visualizing time-varying multichannel EEG data is studied by ten Caat and Roerdink (2007). Johansson et al. (2008) investigate the amount of noise that may be present in parallel coordinates such that patterns can still be received. Holten and van Wijk (2010) evaluate cluster identification performance for curved and animated parallel coordinates, among others. While Li and van Wijk (2010) examined the visualization of correlation for linear parallel coordinates and Holten and van Wijk (2010) the visualization of clusters, our user study aims at evaluating the impact of bundling and curves to the judgment of correlation and the detection of clusters.

Finally, there seems to be no literature concerning the evaluation of bundling at all.

3 USER STUDY

To compare the effectiveness of polylines and bundled curves, we performed a user study. Observers were asked to estimate (a) correlations and (b) the number of clusters, in datasets represented using polylines and bundled curves. We expected that bundled curves would support correlation estimation at least as well as polylines do, and that bundled curves would support superior estimation of the number of clusters.

3.1 Overview

In designing the experiment, we were subject to the constraint that we needed to estimate performance by analysts skilled both in an underlying domain and at interpreting parallel coordinates a given type, polyline or bundled curves. Such users are not merely difficult to find, for the case of bundled curves they do not yet exist. We addressed this constraint with an approach often used for visualization user studies. Specifically we:

1. Recruited participants who had little to no experience with either form of parallel coordinates. We gave the participants a short tutorial on strategies for estimating correlations in parallel plots of each style. This created a pool of participants equally skilled at reading both styles, somewhere between novice and intermediate skill.

2. Used data sets generated solely according to specified probability distributions, with no underlying
semantics. This ensured that no participant would be able to apply domain knowledge to interpret the plots.

We used accuracy as the sole dependent measure and did not record time. We argue that this untimed task matches the context in which data analysts typically use parallel coordinates, taking enough time to consider their data in depth. This choice emphasized that participants take as long as necessary to make their best estimate. It also minimized fatigue by allowing participants to rest whenever they wished, without regard for their score. This choice also eliminated the potential confound of different participants adopting different speed-accuracy tradeoffs, because accuracy was uniformly emphasized.

Given the limited experience of the participants with the two styles of plot, we do not believe that timing data would provide any useful comparison between the styles. Comparative timing data would only be informative with testers who were well-experienced with the methods, working on data sets for which they had domain expertise.

The curve styles were compared for two tasks, estimating correlation and estimating number of clusters. The tasks were performed in a fixed order for every participant, with participants estimating correlation first. This design permits more direct interpretation of the results because all participants performed each task with a fixed level of prior experience. In particular, their experience reading plots in the correlation task would carry over to enhance their performance in the cluster estimation task.

By contrast, a design that counterbalanced task order would have split participants’ prior experience, increasing the variance and making the results harder to interpret. Given that a counterbalanced design would only protect against the case that doing the correlation estimate first would differentially advance one curve style, a prospect we consider highly unlikely, we chose a fixed task order for its more straightforward interpretation.

3.2 Design

The study design was single-factor, two-level, and within-subjects. Observers viewed two data series. The first was always the correlation estimation series, the second the cluster estimation series. Within each series, line style was a blocked factor, with all trials performed first in one line style, then the other. Order of the two line styles was counterbalanced across participants, with participants randomly assigned to the order. Dependent measures, computed separately for each series, were the Pearson correlation $r$ between the actual dataset correlation and the correlation estimated by participants, and the Fleiss $\kappa$ measure of agreement amongst participants.

The visualization used for the study requires two parameters to be set. The parameter $\alpha$ defines the smoothness of a curve while the bundling strength $\beta$ controls the extent to which a curve is pulled towards the centroid of its cluster (Heinrich et al., 2011b). Before running the full study, we ran a pilot study with five participants to determine the best values of these parameters. The values $\beta = 0.8$ and $\alpha = 1/6$ achieved the best balance of correlation detection and cluster visualization. These values were used for the bundled plots in both series of trials.

3.2.1 Participants

A convenience sample of 14 participants (9 men, 5 women, ages 23–37) was recruited from graduate students in computing science and engineering science at Simon Fraser University. Of these 14, 2 had previously used polyline parallel coordinates, 8 had experience with some form of information visualization but had never used parallel coordinates, and 4 had never used any visualization software. Volunteers were paid CDN$ 20.

3.2.2 Procedure for the session

Participants first answered a brief series of questions assessing their level of experience with information visualization and computers in general. They were next tested for any color deficiencies using a Web-based test\(^2\). All 14 participants had acceptable color vision. They next read a tutorial on the basic principles of parallel coordinates and their instantiation in polylines and bundled curves. The tutorial defined correlation and gave examples of positive and negative correlation using both line types.

Participants then began the first series of trials, in which they estimated correlations. Immediately after completing that series, participants began the second series, in which they estimated the number of clusters in plots. After completing the second series, they indicated which line style they preferred and answered a short list of open-ended questions about their experience during the study.

Participants were allowed to take as long as they wished on each trial. Total time to complete the session varied widely, from 50 to 110 minutes. Most participants completed the study in less than 90 minutes.

\(^2\)http://www.healthcommunities.com/color-vision-deficiency/color-blindness-test.shtml
3.3 First series: estimating correlations

In the correlation estimation trials, participants viewed a series of datasets in 2D parallel coordinates (i.e., with two data dimensions and two main parallel-coordinates axes), plotted in either polylines or bundled curves. For each plot, the user was asked to categorize the correlation as “strong negative correlation”, “negative correlation”, “no correlation”, “positive correlation”, or “strong positive correlation”.

3.3.1 Procedure

Before starting each line style, participants read a short tutorial on estimating correlations in that style. For polylines, the tutorial suggested looking for whether the lines crossed or not, the distribution of line crossings (whether only in the middle or distributed throughout the range), and the overall shape of the plot. For bundled curves, the tutorial suggested looking at the width of the middle band and the overall shape of the plot. For each style, the tutorial presented example plots of all seven degrees of correlation. To map the seven values of actual correlation to the five categories of user response, the tutorial recommended reporting \( z \) values of \(-1.0\) and \(-0.5\) as both “negatively correlated”, and similarly for \(+0.5\) and \(+1.0\).

Participants began each line style with a training session. The training session presented one plot of each correlation level in the given style. Participants estimated the correlation and were then told which answers would have been appropriate for the dataset. Since there were seven levels of correlation but only five levels of user response, two possible answers were suggested for every example. After estimating all seven practice correlations, a page was displayed reminding participants of the strategies for estimating correlation for this plot style. Users pressed a button to start the first experimental trial.

Experimental trials had the same interface as the practice trials, but provided no feedback about the actual correlation. When the participant was satisfied with their estimate for the current trial, they pressed a button to start the next.

3.3.2 Trial data

Three groups of seven datasets were generated, each with \( n = 40 \) data pairs. The pairs were generated from normally distributed random series \( x \) and \( y \), selected to ensure that each set of 40 pairs had the given correlation coefficient. Each group of datasets had exactly one set for each level

\[
\begin{align*}
z &= -1.5, -1.0, -0.5, 0.0, +0.5, +1.0, +1.5,
\end{align*}
\]

where \( z \) is the Fisher transform of the correlation. These were the same levels of correlation used in prior work (Li et al., 2010). One group of datasets was always used for the training phase. The remaining 14 datasets were each used twice, once for each line style. Within each line style, order of datasets varied randomly for each participant.

The bundled curve representation required two additional parameters for each data point: the directions of the line leaving each axis. These are not required for polyline plots, where the direction of the line leaving an axis is independent of the direction the line entered that axis from the other side. However, the exit direction of bundled curves is affected by the direction of the line entering from the other side, due to the \( C^1 \) continuity requirement. Pilot tests showed that if all curves entered the axes at a constant horizontal direction, observers used the consistent bending of curves at the axes as a cue to estimate correlation. Since this cue would not occur in actual use of bundled curves, which would in fact enter their axes at varying angles, the direction at which each curve entered each axis was randomly perturbed. This random perturbation likely made correlation detection slightly more difficult for bundled curves than it would be in practice, where entry to the axes would vary but not be random.

Figure 2 illustrates example datasets with all seven different correlation coefficients used for the experimental trials. The top row shows polyline plots and the bottom row shows bundled curve plots. The Fisher transform of correlation is shown below each plot.
3.4 Second series: estimating clusters

In the cluster estimation trials, participants viewed a series of clustered datasets in parallel coordinates ranging from two to six dimensions, plotted in either polylines or bundled curves. Clustering was indicated by color (for polyline plots) and bundling (for bundled curve plots). Color Brewer (Harrower and Brewer, 2003) was used to define effective color maps for the polyline plots. For each plot, the user was asked to estimate the number of clusters.

3.4.1 Procedure

Before starting the series, participants read a description of how clusters are represented in both line styles. They then began working with either polyline plots or bundled curve plots, depending upon which order had been assigned. They practiced estimating the number of clusters in three trial plots, with five, three, and eight clusters. Figure 3 shows typical examples of such plots. After each training trial, the correct number of clusters was reported. After the three training trials, a page redisplayed the three datasets and the number of clusters in each. Users pressed a button to start the first experimental trial.

Experimental trials had the same interface as the training trials, but provided no feedback about the actual number of clusters. After entering their estimate for the clusters, participants pressed a button to move on to the next trial. Once they had completed a series in one line style, they did the training and experimental trials for the next style.

3.4.2 Trial data

Trial datasets were created from three real-world and three synthetic datasets (Table 2). The real-world datasets are popular test datasets, taken from the Xmdv Web page3. The synthetic datasets were generated by sampling normally distributed series, selected to ensure the required correlation across each dimension. Each of the 6 datasets was then clustered by the $k$-means technique into $k = 3, 5, 7,$ and $9$ clusters. This series of 24 datasets was plotted using both line styles. Within each series, the order of trials varied randomly for each user.

Table 2: Datasets for the Cluster Estimation Series ($d$ is the number of dimensions, $n$ is the number of data points)

<table>
<thead>
<tr>
<th>Name</th>
<th>$d$</th>
<th>$n$</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>iris</td>
<td>4</td>
<td>150</td>
<td>Botany</td>
</tr>
<tr>
<td>netperf</td>
<td>6</td>
<td>179</td>
<td>Computer Science</td>
</tr>
<tr>
<td>htong</td>
<td>4</td>
<td>365</td>
<td>Earth Science</td>
</tr>
<tr>
<td>g40</td>
<td>2</td>
<td>40</td>
<td>Synthetic</td>
</tr>
<tr>
<td>g160</td>
<td>3</td>
<td>160</td>
<td>Synthetic</td>
</tr>
<tr>
<td>g200</td>
<td>5</td>
<td>200</td>
<td>Synthetic</td>
</tr>
</tbody>
</table>

3.5 Results

Figure 4 shows the distribution of participants’ responses for the correlation estimation series. There was a strong linear correlation between participants’ estimates and actual correlation for polylines and bundled curves (both $r = 0.90$). Considering the estimates for positive and negative correlations separately, estimates for negative correlations were stronger ($r = 0.75$ for polylines, $r = 0.79$ for bundled curves, difference of the equivalent $z$-scores $\Delta z = 0.10$) than for positive correlations ($r = 0.55$ for polylines, $r = 0.39$ for bundled curves, $\Delta z = -0.21$). Agreement amongst participants was moderate.

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3http://davis.wpi.edu/xmdv/datasets.html
The results for polylines are comparable to those of Li and van Wijk (2010).

For all comparisons the one-sided width of a 95% confidence interval, which is entirely determined by the sample size of 14, is $\Delta_{2.58} = 0.59$. All the $\Delta$ scores presented above were substantially within this bound, indicating that none of the differences was statistically significant.

Figure 4 shows the distribution of participants’ responses for the estimated correlations of 2D parallel coordinates for polylines and bundled curve plots. Circle radius represents the frequency with which participants estimated a correlation strength for each actual correlation.

Figure 5 shows the distribution of participants’ responses for the cluster estimation series. The overall correlation is strong for both line styles ($r = 0.92$ for polylines, $r = 0.96$ for bundled curves, $\Delta = 0.36$). The correlations were much stronger for datasets with three or five clusters ($r = 0.98$ for both line styles) than those with seven or nine clusters ($r = 0.41$ for polylines, $r = 0.68$ for bundled curves, $\Delta = 0.39$).

As with the correlation estimation series, all $\Delta$ values were substantially below 0.59, indicating that none of the differences was statistically significant.

Agreement amongst participants for cluster estimation was slightly higher for bundled curves ($\kappa = 0.65$) than for polylines ($\kappa = 0.56$). Each line style had higher agreement than their corresponding levels for correlation estimation.

### 3.6 Discussion

The results for the two series of plots demonstrate important strengths of the bundled curve representation. The correlation estimation series demonstrates that correlation is as readily recognizable when parallel coordinates are rendered in bundled curves as when rendered in polylines. This result is not obvious. Polylines provide a clear focal point for estimating correlations: the width of the center region is an excellent indicator of correlation, with strong negative correlations producing a narrow center region and strong positive correlations producing a wide center region. In contrast, bundled curve plots by definition draw the curves into one or more narrow center regions. The width of those regions is only mildly determined by the correlation of the dataset. Yet bundled curves nonetheless provided sufficient cues (width of center region, shape of lines) that participants could estimate correlation from bundled curves as readily as from polylines.

The cluster counting series demonstrates that viewers could identify clusters through their bundles. This is not surprising, as bundling provides a strong cue of cluster identity. Participants likely determined cluster membership by looking at the bundle axes, where bundling has its strongest effect. In effect, a bundled curve plot uses different regions to geometrically represent the spread and the clustering of the dataset. The spread of values for a cluster is represented at the value axis. The cluster identity of a datum is represented at the bundle axis. In contrast, polylines provide no geometric representation of cluster membership, so it must be represented using a different cue, color. Whereas polylines provide only correlation information in the inter-axis regions, bundled curves use that region to display correlation, number of clusters, and cluster membership—a much more effective use of the space.

The geometric representation of cluster and distribution must be simultaneous if the analyst is to compare the distributions of the different clusters. The bundling and $C^1$ continuity of bundled curves are essential for this comparison to occur, for these features allow the viewer to be aware of both clusters and distribution simultaneously. Bundling exploits the Gestalt principle of proximity, visually grouping the lines of a cluster in the middle of the plot. $C^1$ continuity exploits the Gestalt principle of continuity to maintain this visual grouping on the value axes, where the distribution is represented. This allows the viewer...
to compare the distributions of different clusters. As a secondary benefit, the $C^1$ continuity allows this cluster identification to be maintained across value axes, the membership reinforced at each bundle axis.

The same bundling strength was used for both the correlation and the cluster counting series. This demonstrates that each task can be achieved without sacrificing the other.

4 CONCLUSION AND FUTURE WORK

The user study conducted in this work supports the following conclusions: Firstly, curve bundling is effective in displaying clustering information purely based on geometry. Secondly, with a properly chosen bundling strength, bundled curve plots retain the same strength as polyline plots in revealing correlations between visualized variables. Hence one of the core aspects of analysis using parallel coordinates carries over using bundling.

The high effectiveness of curved plots compared with polyline plots was not obvious. The results of our user study might trigger further perceptual investigations of variants of parallel-coordinates plots. It could be the case that other forms of parallel-coordinates plots might be even more effective than bundled curves—not only for cluster visualization but other applications.

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